

Bibliography

- [1] P.J. Bickel and K.A. Doksum, *Mathematical Statistics: Basic Ideas and Selected Topics*, Prentice Hall, 1977.
- [2] J. Boyle, RSVP Extensions for CIDR Aggregated Data Flow, Internet work in progress, June 1997.
- [3] K. Gopalan and T. Chiueh, *Delay Budget Allocation in Delay Bounded Network Paths*, Technical Report TR-113, Experimental Computer Systems Labs, Dept. of Computer Science, State University of New York, Stony Brook, NY, June 2002.
- [4] D. Mitra and Q. Wang, Stochastic Traffic Engineering, with Applications to Network Revenue Management, *Proceedings of IEEE INFOCOM'03*, San Francisco, 2-10, CA, 2003.
- [5] MATLAB 6.5, the Mathworks, Inc., 2002.
- [6] E. Mulyana, U. Killat, A Hybrid Genetic Algorithm Approach for OSPF Weight Setting Problem, *2nd POLISH-GERMAN TELETRAFFIC SYMPOSIUM PGTS, 9th Polish Teletraffic Symposium*, 2002, found in internet.
- [7] E. Mulyana and U. Killat, An Alternative Genetic Algorithm to Optimize OSPF Weights, July 2002, found in internet.
- [8] W. Ogryczak, T. Śliwiński and A. Wierzbicki, Fair Resource Allocation Schemes and Network Dimensioning Problems, *Journal of Telecommunication and Information Technology*, 34-42, Mar. 2003.
- [9] A. Orda, Routing with End-to-End QoS Guarantees in Broadband Networks, *IEEE/ACM Transaction on Networking*, Vol. 7, No. 3, 365-374,

June 1999.

- [10] K.G. Ramakrishnan and M.A. Rodrigues, Optimal Routing in Shortest Path Data Networks, *Bell Labs Technical Journal*, 117–138, January, June 2001.
- [11] S. Rooney, Connection closures: Adding application-defined behavior to network connections, *Internet work in progress*, April 1997.
- [12] P. Thomas, D. Teneketzis, J. K. Mackie-Mason, A Market-Based Approach to Optimal Resource Allocation in Integrated-Services Connection-Oriented Networks, *Operations Research*, Vol. 50, No. 4, 603-616, July-August 2002.
- [13] C.H. Wang, Mathematical Models of Pareto Optimal Path Selection on All-IP Networks, Master Thesis, National Chengchi University, Taipei, 2004.
- [14] L. W. Winston, *Operations Research Applications and Algorithms*, Belmont, CA: THOMSON BROOKS/COLE, 2004.

Appendix A.

Lehmann-Scheffé theorem of what distribution: Let X be a random vector having density $f(x; \theta)$.

Consider a model with a complete sufficient statistic $T=G(X)$.

- a. If $h(T)$ is an unbiased estimator of $\tau(\theta)$, it is the best unbiased estimator of $\tau(\theta)$.
- b. The best unbiased estimator is unique.
- c. If there is any unbiased estimator of $\tau(\theta)$, there is a best unbiased estimator of $\tau(\theta)$.

Appendix B.

Random number generator based on the Poisson distribution:

Step 1 Let $a = e^{-10}$, $b = 1$, and $c = 0$.

Step 2 Generate $U_{c+1} \sim U(0, 1)$ and replace b by bU_{c+1} . If $b < a$ return $X = c$ otherwise go to **step 3**.

Step 3 Replace c by $c+1$ and go back to **step 2**.

Appendix C.

The Ford-Fulkerson Method for Solving Maximum Flow Problems

Given a feasible flow, how can we tell if it is an optimal flow? We determine which of the following properties is possessed by each arc in the network [14]:

Property 1 The flow through arc e is below the capacity of arc e . In this case, the flow through arc e can be increased. For this reason, we let S represent the set of arcs with this property.

Property 2 The flow in arc e is positive. In this case, the flow through arc e can be reduced. For this reason, we let R be the set of arcs with this property.

Now we can describe the Ford-Fulkerson labeling procedure used to modify a feasible flow in an effort to increase the flow from the source to the sink.

Step 1 Label the sources.

Step 2 Label nodes and arcs according to the following rules:

- (1) If node j_1 is labeled, node j_2 is unlabeled and arc e is a member of S : label node j_2 and arc e . In this case, arc e is called a forward arc.
- (2) If node j_1 is unlabeled, node j_2 is labeled and arc e is a member of R : label node j_1 and arc e . In this case, e is called a backward arc.

Step 3 Continue this labeling process until the sink has been labeled or until no more vertices can be labeled.

If the labeling process result in the sink being labeled, we can obtain a new feasible flow that has a larger flow from source to sink than the current feasible flow; and if the sink cannot be labeled, the current flow is optimal.